


Year:		8	Subject:	Maths	Autumn 1	Autumn 2	Spring 1	
Intent	Subject Concepts (Substantive knowledge) (Key facts and concepts) 	5 Concept areas: 1) Number 2) Algebra 3) Geometry & Measure 4) Statistics & Probability 5) Ratio & Proportion	Unit 1: Number <ul style="list-style-type: none"> Division with single digit and two-digit numbers Order of operations Squaring and cubing numbers Inverse of squaring and cubing numbers Prime factor decomposition 	Prior Knowledge: <ul style="list-style-type: none"> Mental methods Calculation methods (+, -, x ÷) Money & time Negative numbers Factors, multiples & prime 	Unit 3: Statistics, graphs, and charts <ul style="list-style-type: none"> Drawing and interpreting different types of charts Averages from different types of tables and charts 	Prior Knowledge: <ul style="list-style-type: none"> Averages from lists & tables Comparing data Line graphs & bar charts 	Unit 5: Real life graphs <ul style="list-style-type: none"> Drawing distance -time graphs Interpreting distance – time graphs Plotting types of graphs 	Prior Knowledge: <ul style="list-style-type: none"> Straight line graphs Statistical graphs Reading off system of axes
			Unit 2: Area and Volume <ul style="list-style-type: none"> Calculating areas of quadrilaterals, including parallelograms and trapeziums Calculating volume of Cubes and cuboids Calculating Surface area of basic 3D solids 	Prior Knowledge: <ul style="list-style-type: none"> Area of squares & rectangles Counting cm² in shapes 	Unit 4: Expressions and equations <ul style="list-style-type: none"> Expanding single brackets by a common factor Solving one step equations Solving two step equations 	Prior Knowledge: <ul style="list-style-type: none"> Function machines Algebraic expressions & simplifying Writing & substituting into formula 	Unit 6: Decimals and ratio <ul style="list-style-type: none"> Ordering decimals Calculating ratio and proportion with decimals 	Prior Knowledge: <ul style="list-style-type: none"> Decimals & rounding Length, mass & capacity Scales & measures Working with decimals Units of measure in area & perimeter Ratio & proportion with whole numbers
				Takeaway Learning: <ul style="list-style-type: none"> Divisibility rules Calculating with negative numbers Powers & roots BIDMAS Multiples & factors using prime decomposition 	Takeaway Learning: <ul style="list-style-type: none"> Pie charts Using tables Stem & leaf diagrams Scatter graphs Misleading graphs 	Takeaway Learning: <ul style="list-style-type: none"> Conversion graphs Distance-time graphs Line graphs Real-life graphs Curved graphs 		
				Takeaway Learning: <ul style="list-style-type: none"> Area of triangle, parallelogram & trapezium Volume of cubes & cuboids 2D representations of 3D Surface area of cubes & cuboids 	Takeaway Learning: <ul style="list-style-type: none"> Algebraic powers Expressions & expanding brackets. Factorising by common factor Solve linear equations using balancing method 	Takeaway Learning: <ul style="list-style-type: none"> Ordering decimals Place value calculations Ratio & proportion with decimals 		
	Disciplinary Knowledge (Problem solving and reasoning)	Unit 1: Number Students currently working at stage 8. Number and Place Value progression map	Unit 2: Area and Volume Students currently working at stage 8. Measurement and mensuration progression map	Unit 3: Statistics, graphs, and charts Students currently working at stage 8. Statistics progression map	Unit 4: Expressions and equations Students currently working at stage 8. Algebra progression map	Unit 5: Real life graphs Students currently working at stage 8. Algebra progression map	Unit 6: Decimals and ratio Students currently working at stage 8. Ratio and Proportion progression map	

Common Misconceptions

Unit 1: Number

- Many pupils believe that 1 is a prime number – a misconception which can arise if the definition is taken as ‘a number which is divisible by itself and 1’.
- Some pupils may think $35\ 934 = 36$ to two significant figures
- When converting between ordinary and standard form some pupils may incorrectly connect the power to the number of zeros, e.g., $4 \times 10^5 = 400\ 000$ so $4.2 \times 10^5 = 4\ 200\ 000$
- Similarly, when working with small numbers (negative powers of 10) some pupils may think that the power indicates how many zeros should be placed between the decimal point and the first non-zero digit

Unit 3: Statistics, graphs, and charts

- Some pupils may label the bar of a histogram rather than the boundaries of the bars.
- Some pupils may think that there are gaps between the bars in a histogram.
- Some pupils may misuse the inequality symbols when working with a grouped frequency table

Unit 5: Real life graphs

- When plotting linear graphs some pupils may draw a line segment that stops at the two most extreme points plotted
- Some pupils may think that a sketch is a very rough drawing. It should still identify key features, and look neat, but will not be drawn to scale.
- Some pupils may think that a positive gradient on a distance-time graph corresponds to a section of the journey that is uphill.
- Some pupils may think that the graph $y = x^2 + c$ is the graph of $y = x^2$ translated horizontally.

Unit 2: Area and Volume

- Some pupils will work out $(\pi \times \text{radius})^2$ when finding the area of a circle.
- Some pupils may use the sloping height when finding cross-sectional areas that are parallelograms, triangles, or trapezia.
- Some pupils may think that the area of a triangle = base \times height
- Some pupils may think that you multiply all the numbers to find the volume of a prism.

Some pupils may confuse the concepts of surface area and volume

Unit 4: Expressions and equations

- Some pupils may think that you always have to manipulate the equation to have the unknowns on the LHS of the equal sign, for example $2x - 3 = 6x + 6$
- Some pupils think if $4x = 2$ then $x = 2$.
- When solving equations of the form $2x - 8 = 4 - x$, some pupils may subtract ‘x’ from both sides.

Unit 6: Decimals and ratio

- Many pupils will want to identify an additive relationship between two quantities that are in proportion and apply this to other quantities in order to find missing amounts.
- Some pupils may think that a multiplier always has to be greater than 1.
- When converting between times and units, some pupils may base their working on 100 minutes = 1 hours

Enabling or Adapting the Curriculum

SEND Students

Unit 1: Number
Lessons and tasks to include:

- Scaffolding worksheets to gradually build to independence.
- Modelled examples
- Sentence starters and writing frames when comparing data.
- Multiplications grids available to support times tables.
- Number lines in classrooms to support counting.
- Long division templates available in lessons
- Short division templates available in lessons
- Long multiplication columns and grids available in lessons

Unit 3: Statistics, graphs, and charts
Lessons and tasks to include:

- Scaffolding worksheets to gradually build to independence.
- Modelled examples
- Sentence starters and writing frames when comparing data.
- Multiplications grids available to support times tables.
- Number lines in classrooms to support counting.
- Using mathematical equipment (ruler, protractor, calculator etc)
- Drawing a straight line
- Using a template to draw graphs and charts.

Unit 5: Real life graphs
Lessons and tasks to include:

- Scaffolding worksheets to gradually build to independence.
- Modelled examples
- Sentence starters and writing frames when comparing data.
- Multiplications grids available to support times tables.
- Number lines in classrooms to support counting.
- Using mathematical equipment (ruler, protractor, calculator etc)
- Drawing a straight line
- Using a template to draw graphs and charts.

Unit 2: Area and Volume
Lessons and tasks to include:

- Scaffolding worksheets to gradually build to independence.
- Modelled examples
- Sentence starters and writing frames when comparing data.
- Multiplications grids available to support times tables.
- Number lines in classrooms to support counting.
- Reminders for formulae

Unit 4: Expressions and equations
Lessons and tasks to include:

- Scaffolding worksheets to gradually build to independence.
- Modelled examples
- Sentence starters and writing frames when comparing data.
- Multiplications grids available to support times tables.
- Number lines in classrooms to support counting.

Unit 6: Decimals and ratio
Lessons and tasks to include:

- Scaffolding worksheets to gradually build to independence.
- Modelled examples
- Sentence starters and writing frames when comparing data.
- Multiplications grids available to support times tables.
- Number lines in classrooms to support counting.
- Using mathematical equipment
- Bar templates available

		<ul style="list-style-type: none"> Using mathematical equipment (ruler, protractor, calculator etc) 	<ul style="list-style-type: none"> Grouping similar items before introducing the idea of collecting like terms and algebra, x, and y Solving problems with a box indicating missing numbers instead of letters. 	<ul style="list-style-type: none"> Fraction walls to support proportion. 				
Disadvantaged Students	<p>Unit 1: Number</p> <p>Lessons and tasks to include:</p> <ul style="list-style-type: none"> Scaffolding worksheets to gradually build to independence. Modelled examples Sentence starters and writing frames when answering problem solving questions. Necessary equipment to support in lessons. Real world examples to provide context 	<p>Unit 3: Statistics, graphs, and charts</p> <p>Lessons and tasks to include:</p> <ul style="list-style-type: none"> Scaffolding worksheets to gradually build to independence. Modelled examples Sentence starters and writing frames when answering problem solving questions. Necessary equipment to support in lessons. Real world examples to provide context 	<p>Unit 5: Real life graphs</p> <p>Lessons and tasks to include:</p> <ul style="list-style-type: none"> Scaffolding worksheets to gradually build to independence. Modelled examples Sentence starters and writing frames when answering problem solving questions. Necessary equipment to support in lessons. Real world examples to provide context 					
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More Able Students	<p>Unit 1: Number</p> <p>Develop and strengthen understanding using reasoning opportunities and probing questions, for example.</p> <ul style="list-style-type: none"> Show me two (three-digit) numbers with the highest common factor of 18. And another. And another... Show me two numbers with the lowest common multiple of 240. And another. And another... Jenny writes $7.1 \times 10^{-5} = 0.0000071$. Kenny writes $7.1 \times 10^{-5} = 0.000071$. Who do you agree with? Give reasons for your answer. 	<p>Unit 3: Statistics, graphs, and charts</p> <p>Develop and strengthen understanding using reasoning opportunities and probing questions, for example.</p> <ul style="list-style-type: none"> Show me a scatter graph with positive (negative, no) correlation. And another. And another. Kenny thinks that 'frequency diagram' is just a 'fancy' name for a bar chart. Do you agree with Kenny? Explain your answer. What's the same and what's different: scatter diagram, bar chart, pie chart? Always/Sometimes/Never: A scatter graph shows correlation 	<p>Unit 5: Real life graphs</p> <p>Develop and strengthen understanding using reasoning opportunities and probing questions, for example.</p> <ul style="list-style-type: none"> Draw a distance-time graph of your journey to school. Explain the key features. Show me a point on this line (e.g., $y = 2x + 1$). And another, and another ... (Given an appropriate distance-time graph) convince me that Kenny is stationary between 10: 00 a.m. and 10:45 a.m. 					
	<p>Unit 2: Area and Volume</p> <p>Develop and strengthen understanding using reasoning opportunities and probing questions, for example.</p> <ul style="list-style-type: none"> Convince me $C = 2\pi r = \pi d$. What is wrong with this statement? How can you correct it? The area of a circle with radius 7 cm is approximately 441 cm^2 because $(3 \times 7)^2 = 441$. Convince me that the area of a semi-circle $= \frac{\pi d^2}{8}$ Name a right prism. And another. And another ... Convince me that a cylinder is not a prism. 	<p>Unit 4: Expressions and equations</p> <p>Develop and strengthen understanding using reasoning opportunities and probing questions, for example.</p> <ul style="list-style-type: none"> Show me an (one-step, two-step) equation with a solution of -8 (negative, fractional solution). And another. And another ... Show me a two-step equation that is 'easy' to solve. And another. And another ... What's the same, what's different: $2x + 7 = 25$, $3x + 7 = x + 25$, $x + 7 = 7 - x$, $4x + 14 = 50$? <p>Convince me how you could use graphs to find solutions, or estimates, for equations.</p>	<p>Unit 6: Decimals and ratio</p> <p>Develop and strengthen understanding using reasoning opportunities and probing questions, for example.</p> <ul style="list-style-type: none"> Show me an example of two quantities that will be in proportion. And another. And another ... (Showing a table of values such as the one below) convince me that this information shows a proportional relationship. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>6</td> <td>9</td> </tr> <tr> <td>10</td> <td>15</td> </tr> <tr> <td>14</td> <td>21</td> </tr> </table> <ul style="list-style-type: none"> Which is the faster speed: 60 km/h or 10 m/s? Explain why. 	6	9	10	15	14
6	9							
10	15							
14	21							

Literacy/Numeracy Skills



LITERACY

Reading:

New vocabulary linked to new concepts.
 Mathematical reading material once a week for 20 minutes
 Use of keywords for example:
 Prime
 Prime factor
 Prime factorisation
 Product
 Venn diagram
 Cross-section
 Cylinder
 Polygon, polygonal
 Solid

New vocabulary linked to new concepts.
 Mathematical reading material once a week for 20 minutes
 Use of keywords for example:
 Scale, Graph
 Axis, axes
 Scatter graph (scatter diagram, scattergram, scatter plot)
 Unknown
 Equation
 Operation
 Solve
 Solution
 Brackets

New vocabulary linked to new concepts.
 Mathematical reading material once a week for 20 minutes
 Use of keywords for example:
 Linear
 Substitute
 Kinematic, Speed, Distance
 Ratio
 Proportion
 Proportional
 Multiplier

Writing:

Writing reasoning with correct punctuation & use of mathematical keywords & symbols
 Example of writing fluency in maths

Prime Factorization of 72:

$$2^3 \times 3^2$$

Writing reasoning with correct punctuation & use of mathematical keywords & symbols
 Example of writing fluency in maths

15, 16, 21, 23, 23, 26, 26, 30, 32, 41

Writing reasoning with correct punctuation & use of mathematical keywords & symbols
 Example of writing fluency in maths

Oracy:

Incidental language based on ability groups.
 Example of spoken fluency in maths

To find the area of a trapezium, add the parallel sides, divide by 2 then multiply by the distance between the parallel sides

$$\text{Area} = \left(\frac{a+b}{2}\right)h = \left(\frac{4+8}{2}\right) \times 3 = 6 \times 3 = 18 \text{ cm}^2$$

Incidental language based on ability groups.
 Example of spoken fluency in maths

$$6x - 5 = 7$$

$$\begin{array}{r} +5 \\ \hline 6x = 12 \\ \div 6 \\ \hline x = 2 \end{array}$$

Incidental language based on ability groups.
 Example of spoken fluency in maths

Comparing Fractions, Decimals and Percentages

Fractions, decimals and percentages are different ways of expressing the same value.

E.g.

$\frac{1}{2} = 0.5 = 50\%$	$\frac{3}{8} = 0.375 = 37.5\%$
$\frac{1}{4} = 0.25 = 25\%$	$\frac{9}{20} = 0.45 = 45\%$
$\frac{3}{5} = 0.6 = 60\%$	$\frac{27}{40} = 0.925 = 92.5\%$

NUMERACY

Number skills
 Numeracy check-up every week
 Numeracy Ninjas / Maths Box weekly check-up (core, support or extend) & staff to reflect on reasoning

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Digital Strategy



Unit 1: Number
[KM: Ben Nevis](#)
[KM: Astronomical numbers](#)
[KM: Interesting standard form](#)
[KM: Powers of ten](#)
[KM: Maths to Infinity: Standard form](#)
[Powers of ten film \(external site\)](#)
[The scale of the universe animation \(external site\)](#)

Unit 3: Statistics, graphs, and charts
[KM: Gathering data](#)
[KM: Spreadsheet statistics](#)
[KM: Stick on the Maths HD2: Selecting and constructing graphs and charts](#)
[KM: Stick on the Maths HD3: Working with grouped data](#)

Unit 5: Real life graphs
[KM: Plotting graphs](#)
[KM: Matching graphs](#)
[KM: Matching graphs \(easy\)](#)
[KM: Autograph 1](#)
[KM: Autograph 2](#)
[KM: The hare and the tortoise](#)

Unit 2: Area and Volume
[KM: Circle connections, Circle connections v2](#)
[KM: Circle circumferences, Circle problems](#)
[KM: Circumference searching](#)
[KM: Maths to Infinity: Area and Volume](#)

Unit 4: Expressions and equations
[KM: Solving equations](#)
[KM: Stick on the Maths: Constructing and solving equations](#)
[NRICH: Think of Two Numbers](#)

Unit 6: Decimals and ratio
[KM: Proportion for real](#)
[KM: Investigating proportionality](#)
[KM: Maths to Infinity: Fractions, decimals, percentages, ratio, proportion](#)

